

THE CATHOLIC UNIVERSITY OF AMERICA
Washington, DC 20064

SEMINAR IN FUNCTIONAL ANALYSIS
AND RELATED AREAS

Wednesday, September 28, 2022

4:45 p.m. - 6:30 p.m. (including a coffee break)

SPEAKER: Professor Neil Hindman
Howard University

TITLE: Pairwise sums and products in \mathbb{R}^+
(Joint research with Maria-Romina Ivan and Imre Leaderwork with Vitaly Bergelson)

ABSTRACT: FS, FP, PS, and PP stand for finite sums, finite products, pairwise sums and pairwise products respectively, all without repetition. Sometime shortly after the big bang it was shown that if a semigroup (S, \cdot) is finitely colored, there are a sequence $\langle x_n \rangle_{1 \leq n < \infty}$ and a color class which contains $FP(\langle x_n \rangle_{1 \leq n < \infty})$.

In 1999, Bergelson, Hindman, and Leader showed that if the real interval $(0, 1)$ is finitely colored and each color class is measurable or each color class has the property of Baire, then there are a sequence $\langle x_n \rangle_{1 \leq n < \infty}$ and a color class which contains $FS(\langle x_n \rangle_{1 \leq n < \infty}) \cup FP(\langle x_n \rangle_{1 \leq n < \infty})$.

The first of our results that I will discuss shows that there is a finite coloring of the positive reals such that each color class is either open or countable (so is measurable and has the property of Baire) and if $\langle x_n \rangle_{1 \leq n < \infty}$ is a sequence with $PS(\langle x_n \rangle_{1 \leq n < \infty}) \cup PP(\langle x_n \rangle_{1 \leq n < \infty})$ monochromatic, then either x_n approaches zero or x_n approaches infinity.

The presentation will be given via Zoom. The corresponding link will be sent to everyone in advance.

ORGANIZERS: V. Bogdan (The Catholic University of America), P. Kainen (Georgetown University), R. Kalpathy (The Catholic University of America), and A. Levin (The Catholic University of America).

Tel: [202-319-5221](tel:202-319-5221), [202-319-5222](tel:202-319-5222). Fax: [202-319-5231](tel:202-319-5231). E-mail: levin@cua.edu

Web page:

<https://mathematics.catholic.edu/faculty-and-research/mathematics-seminar/index.html>